## Proportion

## Mark Scheme

| Level | IGCSE |
| :--- | :--- |
| Subject | Maths |
| Exam Board | Edexcel |
| Topic | Equations, Formulae and Identities |
| Sub Topic | Proportion |
| Booklet | Mark Scheme |


| Time Allowed: | 59 minutes |
| :--- | :---: |
| Score: | $/ 49$ |
| Percentage: | $/ 100$ |

Grade Boundaries:

| $A^{*}$ | A | B | C | D | E | U |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $>85 \%$ | $75 \%$ | $70 \%$ | $60 \%$ | $55 \%$ | $50 \%$ | $<50 \%$ |


| $\begin{array}{c}\text { Question } \\ \text { Number }\end{array}$ | Working | Answer | Mark | Notes |
| :---: | :--- | :---: | :---: | :---: | :---: |
| 1. (a) | $P=k Q^{3}$ |  | 3 | M1 for $P=k Q^{3}$ but not for $P=Q^{3}$ |$]$



| 3. (a) |  | $81 a^{8} b^{4}$ | 2 | B 2 | B 1 for 81 B1 for $a^{8} b^{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) |  | $3 c^{4}$ | 2 | B 2 | B 1 for 3 B1 for $c^{4}$ |
|  |  |  |  |  |  |


| 4. (a) | $t=k f^{2}$ |  | 3 | M1 for $t=k f^{2}$ but not for $t=f^{2}$ <br> Also award for correct equation in $t, f^{2}$ and a constant or for $t=$ some numerical value $\times f^{2}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 0.02=k \times 8^{2} \text { or } \\ & k=\frac{1}{3200} \text { or } \\ & k=0.0003125 \text { or } \\ & 3.125 \times 10^{-4} \end{aligned}$ |  |  |  | for $0.02=k \times 8^{2}$ or for correct substitution into an equation which scores the first method mark (may be implied by correct evaluation of the constant) |
|  |  | $\begin{aligned} & \quad t=0.0003125 f^{2} \\ & \text { or } t=\frac{1}{3200} f^{2} \end{aligned}$ |  | A1 | Award 3 marks if answer is $t=k f^{2}$ but $k$ is evaluated in part (b) |
| (b) | $\begin{aligned} & f^{2}=\frac{0.0098}{0.0003125} \text { or } \\ & f^{2}=\frac{0.0098}{0.02} \times 8^{2} \end{aligned}$ |  | 2 |  | for substitution and rearrangement into form $f^{2}=\frac{0.0098}{k}$ with their value of $k$ except for $k=1$ or $f^{2}=\frac{0.0098}{0.02} \times 8^{2}$ |
|  |  | 5.6 oe |  | A1 |  |
|  |  |  |  |  | Total 5 marks |


| 5. (a) | $y=k x^{3}$ or $k y=x^{3}$ |  | 3 | M1 | for $y=k x^{3}$ but not for $y=x^{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $250=1000 k$ |  |  |  | for $250=1000 k$ <br> Also award for $250=k \times 10^{3}$ |
|  |  | $y=\frac{1}{4} x^{3}$ oe |  |  | for $y=\frac{1}{4} x^{3}$ oe <br> Award 3 marks if answer is $y=k x^{3}$ and $k$ is evaluated as $\frac{1}{4}$ <br> oe in part (a) or part (b) |
| (b) | $54=" \frac{1}{4} " x^{3}$ |  | 2 | M1 | dep on at least first M1 in part <br> (a) |
|  |  | 6 |  | A1 | ft from $x^{3}=54 \div \frac{1}{4}{ }^{\prime \prime}$ oe |
|  |  |  |  |  | Total 5 marks |


| Question | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6. (a) | $D=k t^{2}$ |  | 3 | M1 for $D=k t^{2}$ but n | for $D=t^{2}$ |
|  | $8=k \times 16$ oe or $8=k \times 4^{2}$ |  |  | M1 |  |
|  |  | $D=\frac{1}{2} t^{2}$ |  | A1 $\quad$ for $D=\frac{1}{2} t^{2}$ oe Award 3 marks i and $k$ is evaluated part (b) | $D$ the subject nswer is $D=k t^{2}$ s $\frac{1}{2}$ in part (a) or |
| (b) | $t^{2}=100$ |  | 2 | M1 |  |
|  |  | 10 |  | A1 Also accept $\pm 10$ | $\begin{aligned} & \mathrm{ft} \text { from } k t^{2}=50 \\ & \text { with } k \neq 1 \end{aligned}$ |
|  |  |  |  |  | Total 5 marks |


| 7. (a) | $\begin{aligned} & v=k \sqrt{x} \text { oe } \\ & 8=k \sqrt{25} \text { oe } \end{aligned}$ | $v=1.6 \sqrt{ } \mathrm{x}$ oe | 3 | M1 <br> M1 <br> A1 Allow $v=k \sqrt{x}$ if $k=1.6$ is found in (a) or (b). |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | $(v=)$ "1.6" $\sqrt{56.25}$ | 12 | 2 | $\begin{aligned} & \text { M1 ft Do not ft if } k=1 \\ & \text { A1 cao } \end{aligned}$ |  |  |
|  |  |  |  |  |  | Total 5 marks |


| Question | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 8. (a) | $F=\begin{gathered} " k " \\ x^{2} \end{gathered}$ |  |  | M1 $k$ must be a letter not a number |
|  | $0.8=\begin{gathered} k \\ 5^{2} \end{gathered} \text { or } k=20$ |  |  | M1 for substitution (implies first M1) |
|  |  | $F=\begin{gathered}20 \\ x^{2}\end{gathered}$ | 3 | A1 Award 3 marks for $F=\begin{gathered}" k " \\ x^{2}\end{gathered}$ and $k=20$ stated anywhere (even in (b)) unless contradicted by later work |
| (b) | $x^{2}=\begin{aligned} & " 20 " \\ & 320 \end{aligned} \text { or } x=\sqrt{\frac{" 20 "}{320}}$ |  |  | M1 ft if $k \neq 1$ for correct rearrangement <br> NB. The only ft is for the value of $k$ in $F=\frac{k}{x^{2}}$ |
|  |  | 0.25 oe | 2 | A1 cao (ignore $\pm$ ) |
|  |  |  |  | Total 5 marks |


| Question | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 9. (a) | $P=k q^{3}$ |  | 3 | M1 Allow $k P=q^{3}$ oe Do not allow $P=q^{3}$ |
|  | $270=k(7.5)^{3}$ oe or $k=\frac{270}{7.5^{3}}$ oe |  |  | M1 for correct substitution in a correct equation. <br> Implies first M1 |
|  |  | $P={ }_{25}^{16} q^{3}$ |  | A1 $\quad P=0.64 q^{3}$ oe with $P$ the subject Award M2A1 if $P=k q^{3}$ on answer line and $k$ evaluated as $\frac{16}{25}$ in part (a) or part (b) |
| (b) | $\operatorname{Eg} q^{2}=\frac{25}{16}$ or $\begin{aligned} & 1 \\ & q^{2}\end{aligned}=\frac{16}{25}$ or $1=\frac{16}{25} q^{2}$ or $q^{2}=\frac{1}{0.64}$ Or $P^{2}=\frac{25}{16}$ or $\frac{1}{P^{2}}=\frac{16}{25}$ or $1=\frac{16}{25} P^{2}$ or $P^{2}=\frac{1}{0.64}$ |  | 2 | M1 Correct equation involving $q^{2}$ or $p^{2}$ $\mathrm{ft} k$ from an equation of the form $P=k q^{3}$ if $k \neq 1$ |
|  |  | $1 \begin{array}{r}1 \\ 4\end{array}$ |  | A1 $\quad \begin{aligned} & 5 \\ & \\ & \\ & 4\end{aligned}, 1.25$ [ignore 0 or negative value.] |
|  |  |  |  | Total 5 marks |


| Question | Working ${ }^{\text {a }}$ Answer |  |  | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10. (a) | $R=\begin{gathered} k \\ c^{2} \end{gathered}$ $30=\begin{gathered} k \\ 4^{2} \end{gathered} \text { or } k=480 \mathrm{oe}$ | $R=\begin{gathered} 480 \\ c^{2} \end{gathered} \text { oe }$ | 3 | M1 <br> M1 <br> A1 | for $R=\begin{aligned} & k \\ & c^{2}\end{aligned}$ but not for $R=\begin{gathered}1 \\ c^{2}\end{gathered}$ <br> Also award for correct equation in $R, c^{2}$ and a constant or for $R=$ numerical value $\div c^{2}$ <br> for $30=\begin{gathered}k \\ 4^{2}\end{gathered}$ or for correct substitution into an equation which scores the first method mark (may be implied by correct evaluation of the constant) <br> Award 3 marks if answer is $R=\begin{gathered}k \\ c^{2}\end{gathered}$ but $k$ is evaluated in part (b). SCB2 for correct formula for $c$ in terms of $R$. |
| (b) | $c^{2}=\frac{480}{1920} \text { or } c^{2}=\frac{30}{1920} \times 4^{2}$ | 0.5 oe | 2 | M1 <br> A1 | M1ft for substitution and rearrangement into form $c^{2}=\frac{k}{1920}$ with their value of $k$ substituted except for $k=1$ accept $\pm 0.5$ |
|  |  |  |  |  | Total 5 marks |

